

# Simulation Studies of Contributions to Event-by-Event Average $p_T$ Fluctuations

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## Outline:

- Data and Observables
- Description of the simulation
- Elliptic Flow Contributions?
- Jet Contributions at RHIC?
- Jet Contributions at CERN?
- Conclusions



# $\langle p_T \rangle$ Fluctuations: Probing for Signs of a Phase Transition

## *Analogy: Critical Opalescence*

A sealed container containing freon on a hot plate at the critical point.  
The image is projected onto a wall.



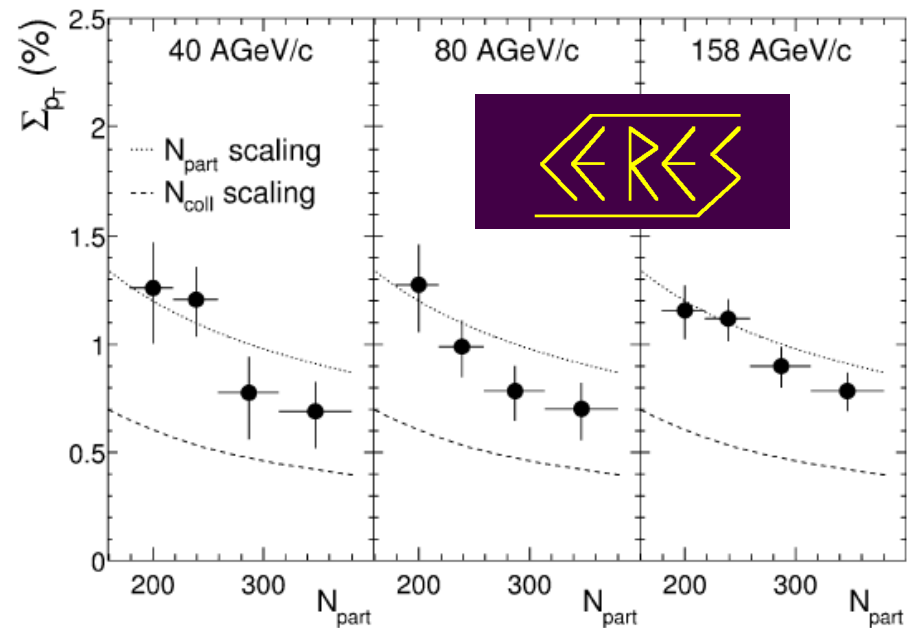
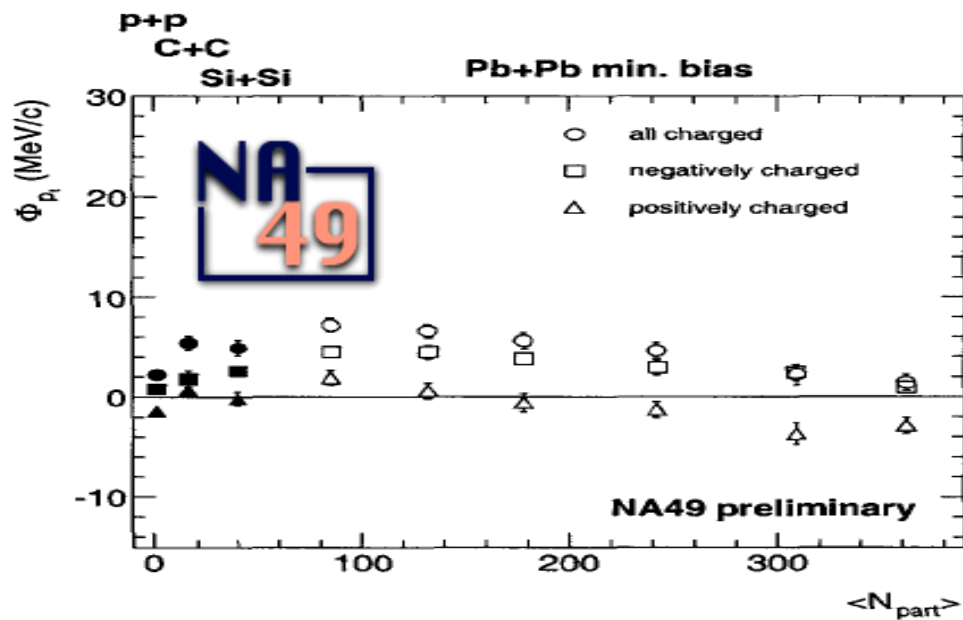
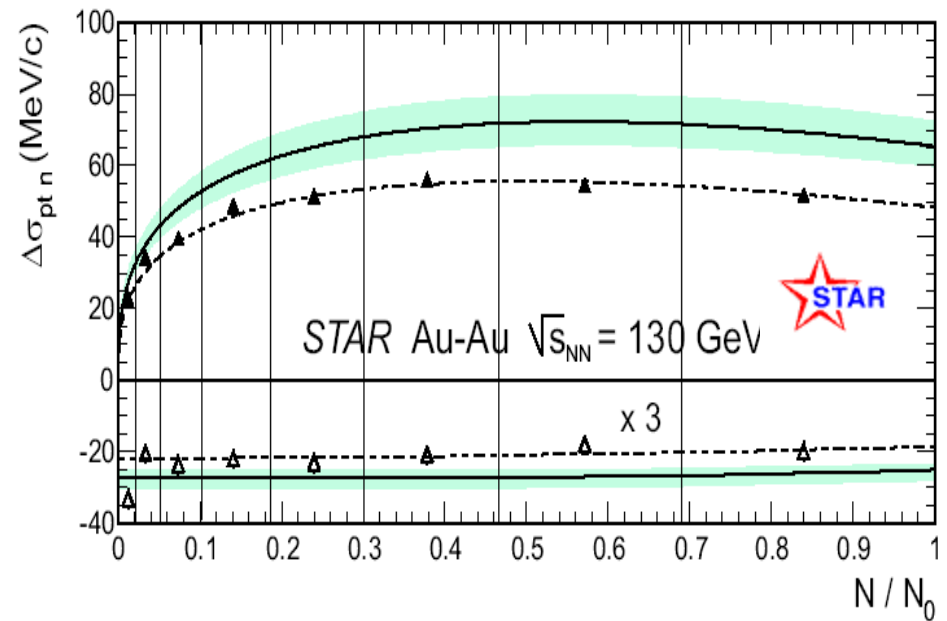
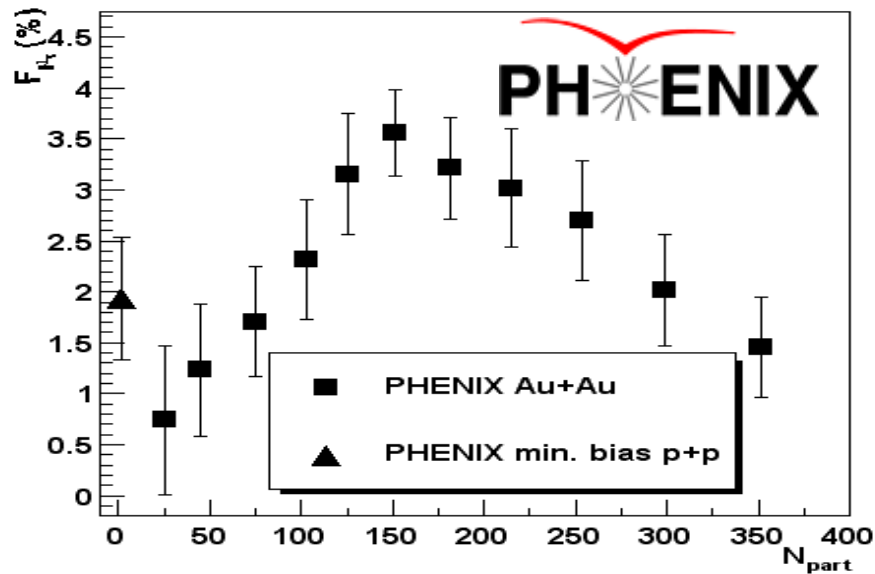
*Movie by the University of Minnesota Physics Department*

- *S. Mrowczynski (see Phys. Lett. B314 (1993) 118.)*

**Instability of the plasma could be present, initiated as random color fluctuations. For some events, the fluctuations of particle transverse quantities would be magnified.**

- *M. Stephanov, et al. (see Phys. Rev. Lett. 81 (1998) 4816)*  
**suggest that near a tri-critical point in the QCD phase diagram, the event-by-event fluctuations in  $p_T$  could increase significantly.**

# Behold The Signal!



# The Pentagon of Fluctuations

Goal of the observables:

State a comparison to the expectation of statistically independent particle emission.

$$\mathbf{F}_{pT} \quad \text{PHENIX}$$

$$\sigma^2_{pT,dyn}$$



$$F_{pT} \approx \frac{\Phi_{pT}}{\sigma_{pT,incl.}}$$

$$\sigma^2_{pT,dyn} \cong \frac{2\Phi_{pT} \sqrt{\Delta p_T^2}}{\langle N \rangle}$$

$$\Delta\sigma_{pT,n} \cong \sqrt{(\Phi_{pT} + \sigma_{pT,incl.})^2 - \sigma_{pT,incl.}^2}$$

$$\Delta\sigma_{pT,n}$$



$$\sigma_{pT,incl.} = \sqrt{\langle p_T^2 \rangle - \langle p_T \rangle^2} \quad \overline{\Delta p_T^2} \equiv \overline{p_T^2} - \overline{p_T}^2$$



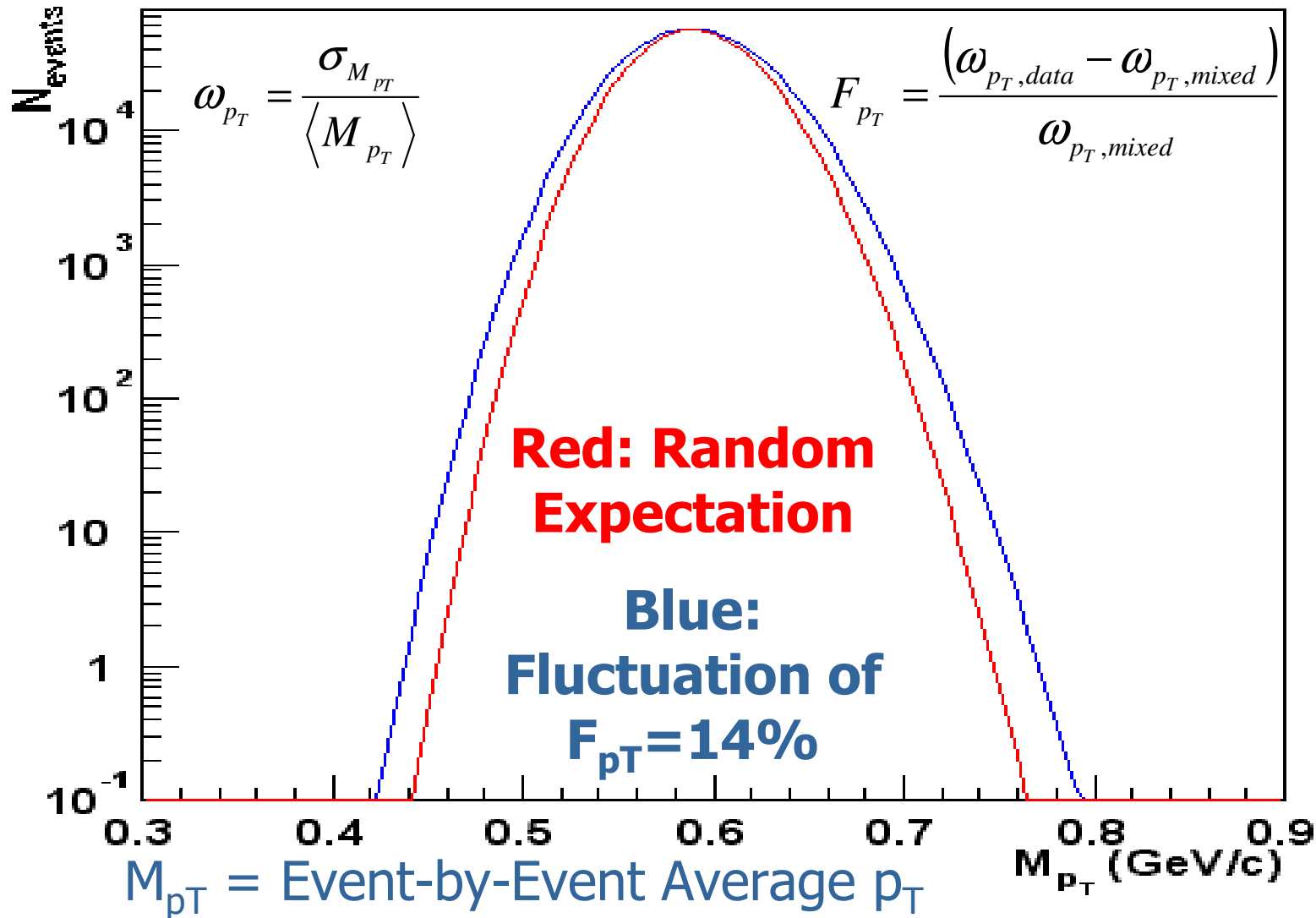
$$\Phi_{pT}$$

$$\Sigma_{pT} \equiv \text{sgn}(\sigma^2_{pT,dyn}) \frac{\sqrt{|\sigma^2_{pT,dyn}|}}{\bar{p}_T}$$



$$\Sigma_{pT}$$

# How To Measure A Fluctuation



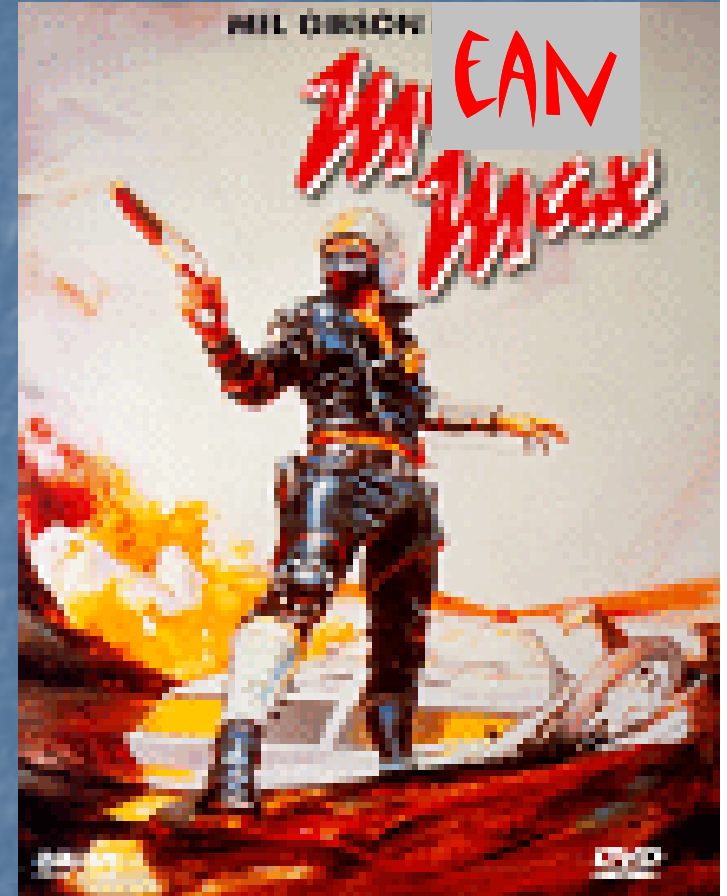


# How To Simulate a Fluctuation: Baseline Simulation

A **data-driven** simulation designed to simulate statistically independent particle production:

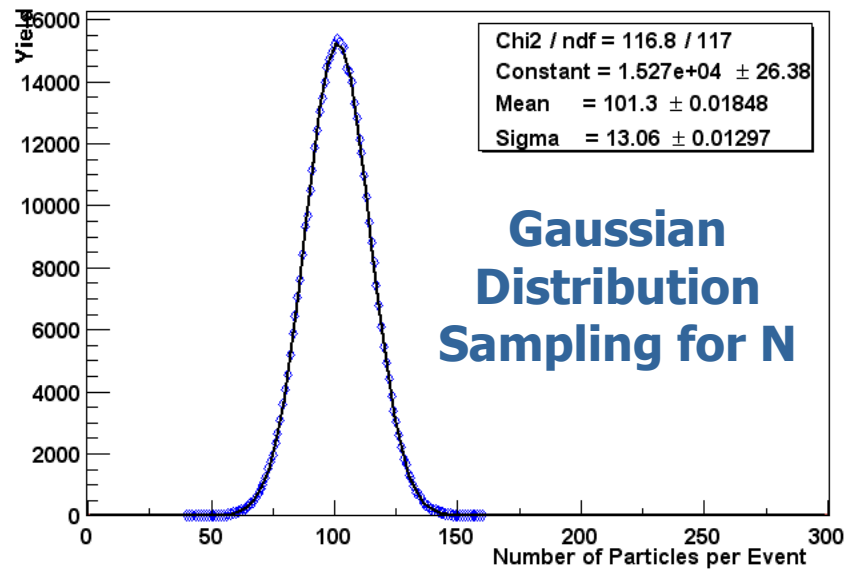
- Generate the number of particles in an event by sampling a Gaussian distribution fit to the data.
- Assign a  $p_T$  to each particle by sampling an  $m_T$  exponential distribution fit (or double exponential, or Gamma distribution) to the data inclusive  $p_T$  distribution.
- Calculates the event-by-event  $\langle p_T \rangle$ ,  $M_{pT}$ .
- Generates mixed events for calculation of fluctuation quantities.

**Input parameters include:  $\langle N \rangle$ ,  $\sigma_{\langle N \rangle}$ , inclusive  $p_T$  function parameters,  $p_T$  range for  $\langle p_T \rangle$  calculation.**

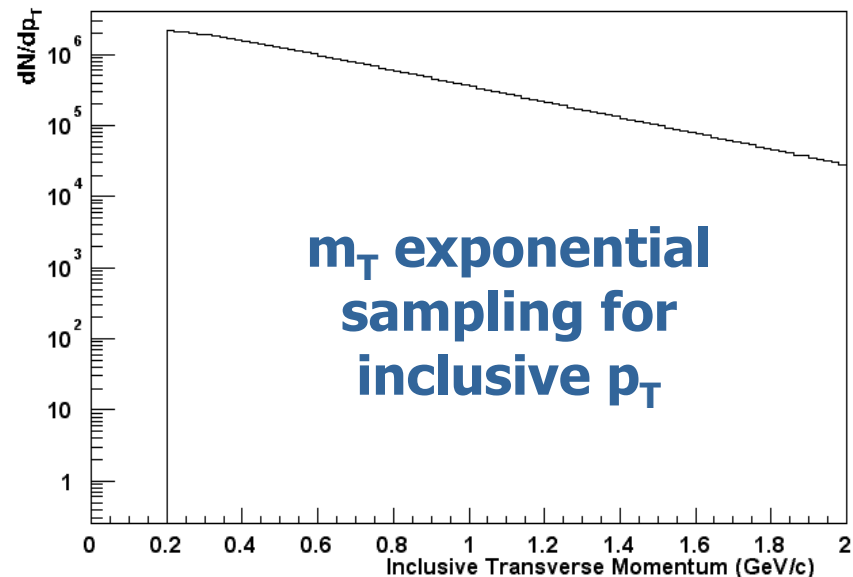


# Results from the Baseline Simulation

Sample: Using  
a match to  
PHENIX 0-5%  
centrality data



Inclusive  $\langle p_T \rangle$ ,  $\sigma_{p_T}$ ,  
 $\langle N \rangle$ ,  $\sigma_{\langle N \rangle}$  matched  
to the data for each  
centrality class.

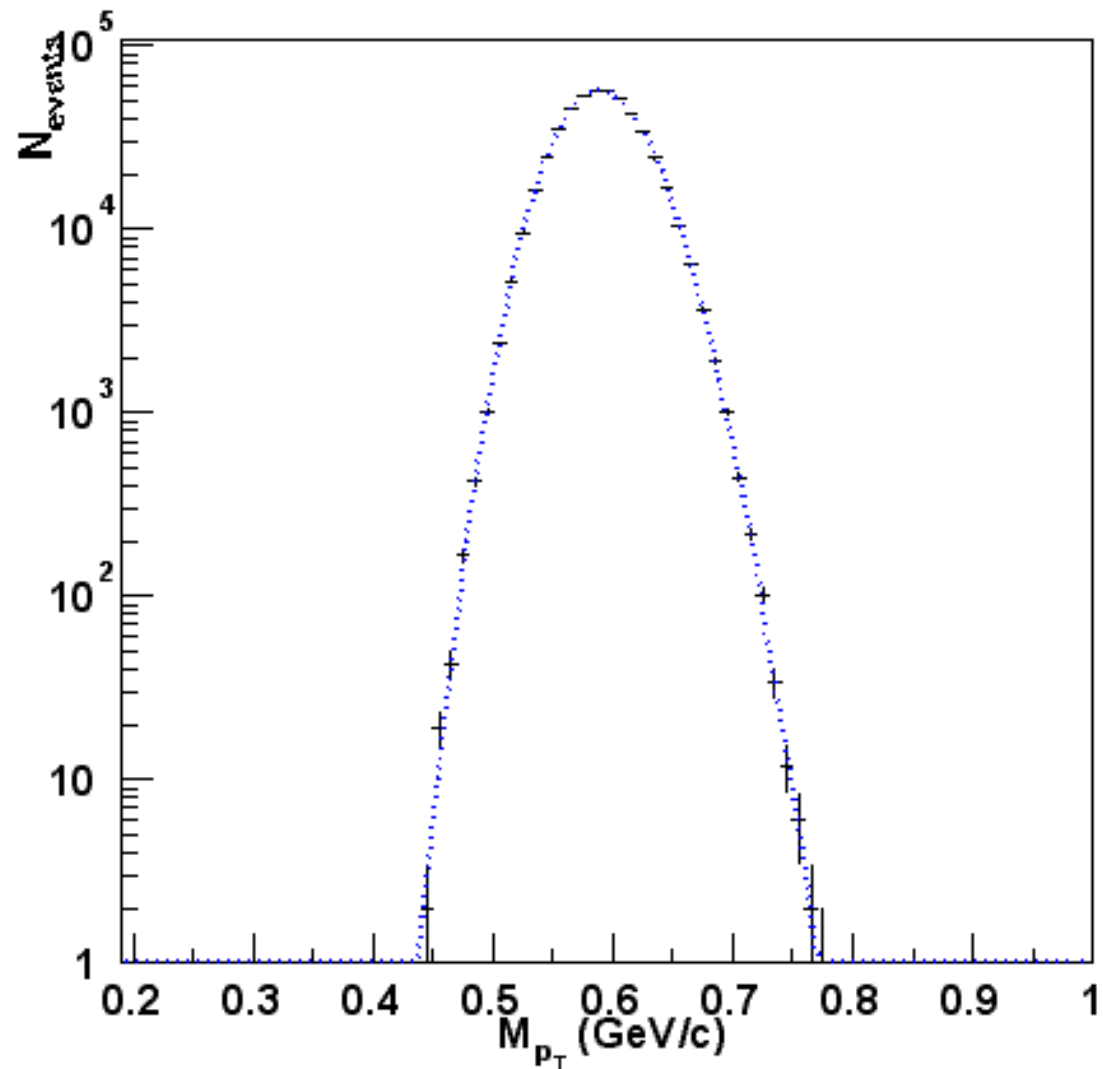


# Results from the Baseline Simulation

Black points: Simulation  
Output

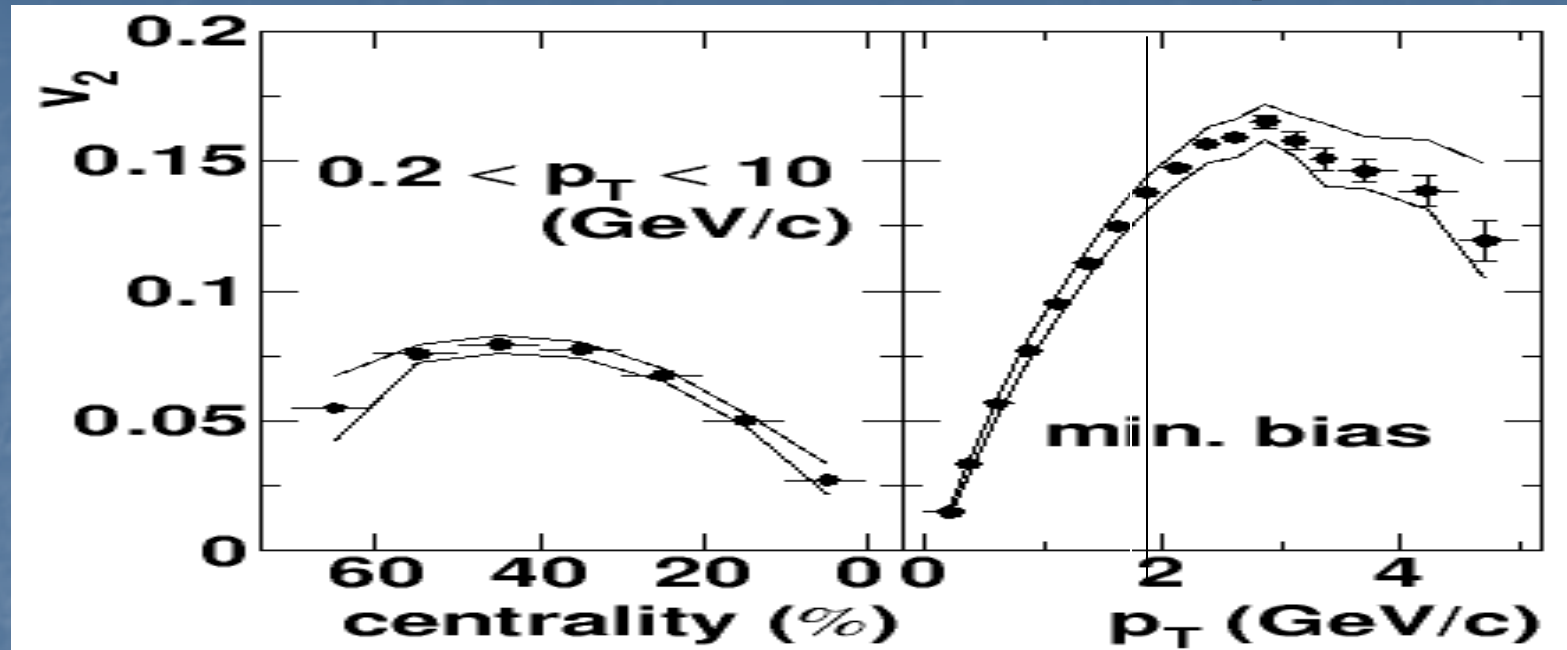
Blue curve: Gamma  
distribution calculation  
for statistically  
independent particle  
emission with input  
parameters taken from  
the inclusive spectra.

*See M. Tannenbaum,  
Phys. Lett. B498 (2001)  
29.*

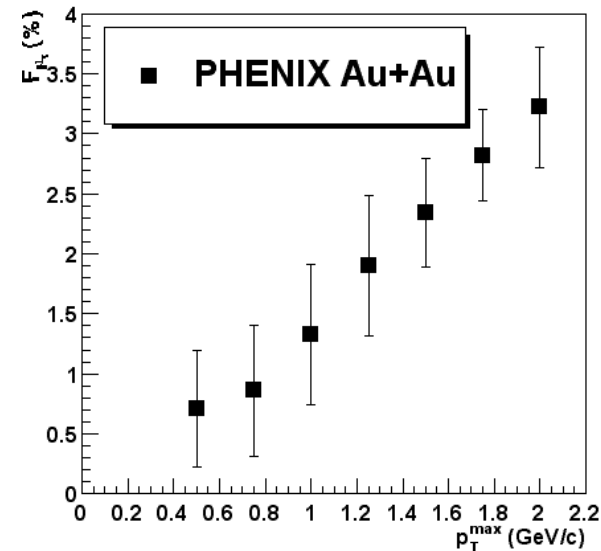
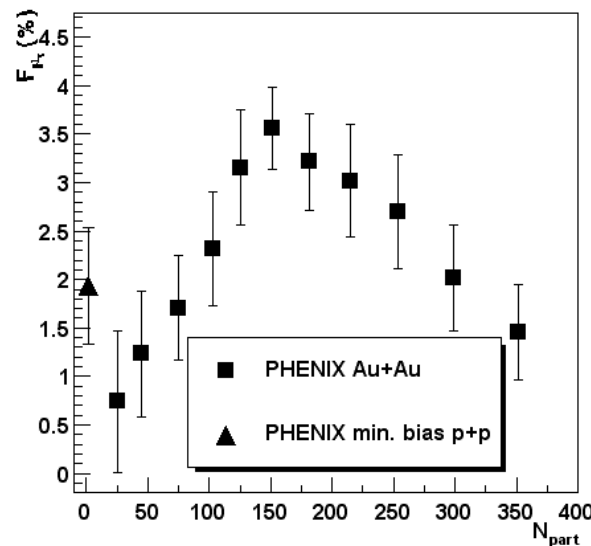




# Fluctuation Trends and Elliptic Flow



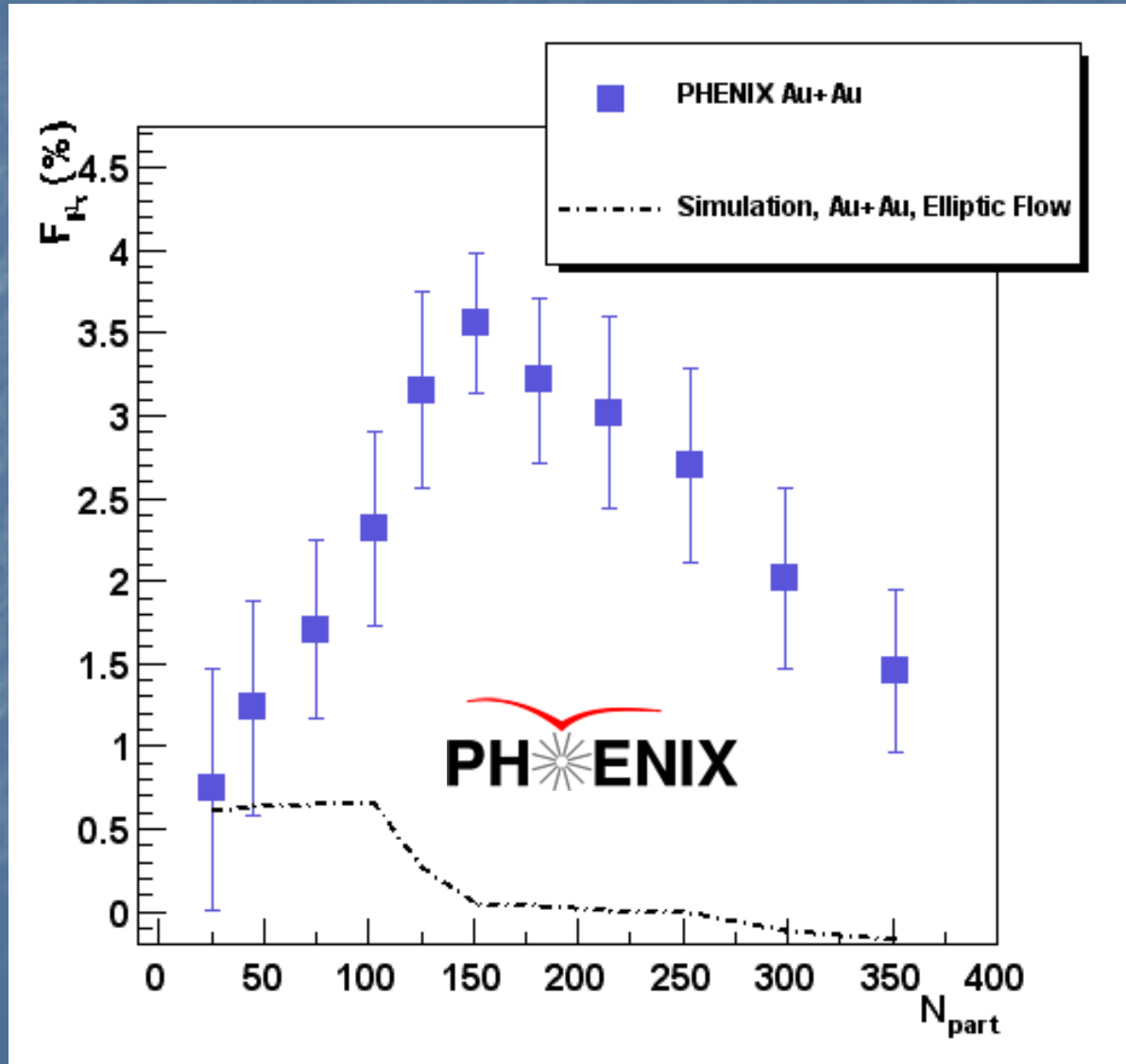
Similar  
properties  
observed  
in PHENIX.



# Elliptic Flow Contribution Simulation

Algorithm: Particles are assigned an azimuthal coordinate based upon the PHENIX measurement of  $v_2$  (wrt the reaction plane) as a function of centrality and  $p_T$ . Only particles within the PHENIX acceptance are included in the calculation of  $M_{pT}$ .

With the exception of peripheral collisions, the elliptic flow contribution is a small fraction of the observed fluctuation.

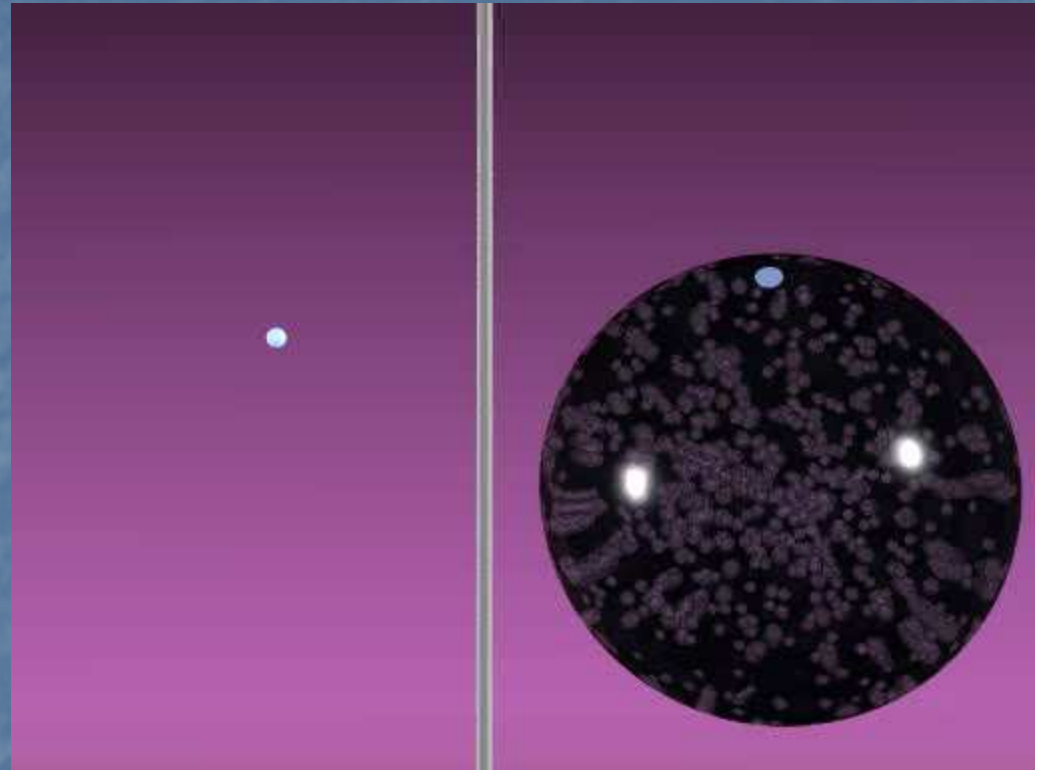


# Fluctuations: A Jet Contribution?

Jets are simulated using a hybrid algorithm which embeds Pythia hard scattering events into Mean Max baseline events.

A single varying parameter is defined: A hard scattering probability factor,  $S_{\text{prob}}$ , is randomly tested for each thrown particle. If the test is true, a single PYTHIA event is embedded into the baseline event after applying experimental acceptance criteria.

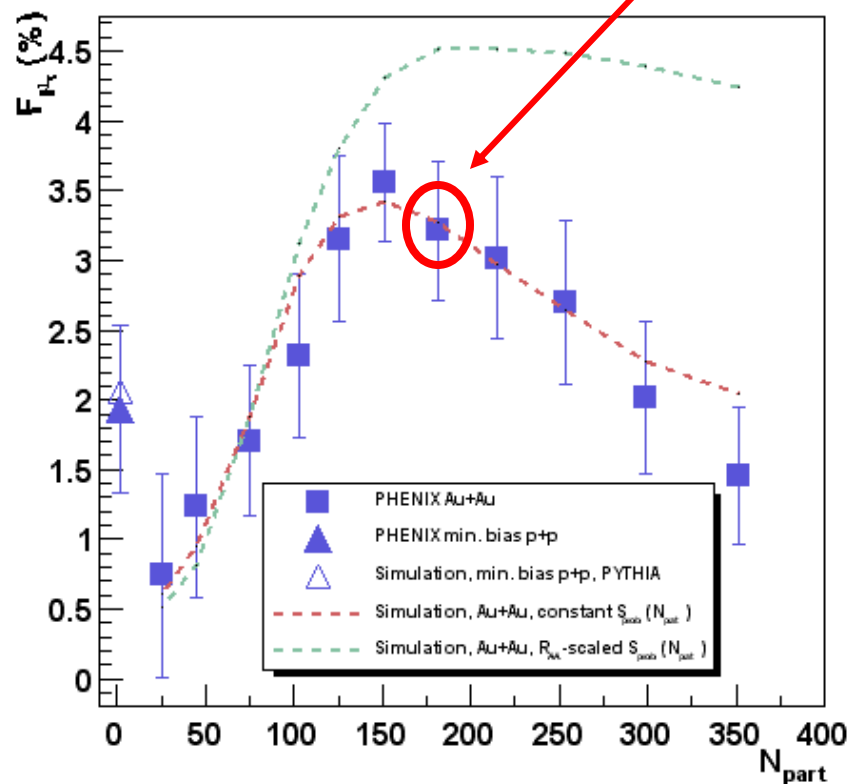
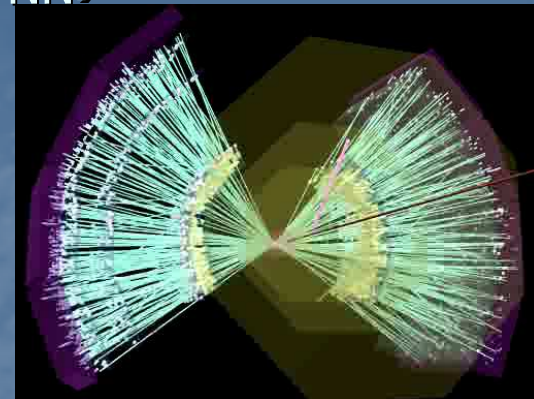
NOTE: The N distribution is preserved in this simulation. The inclusive  $\langle p_T \rangle$  and  $\sigma(p_T)$  are affected by less than 1%.



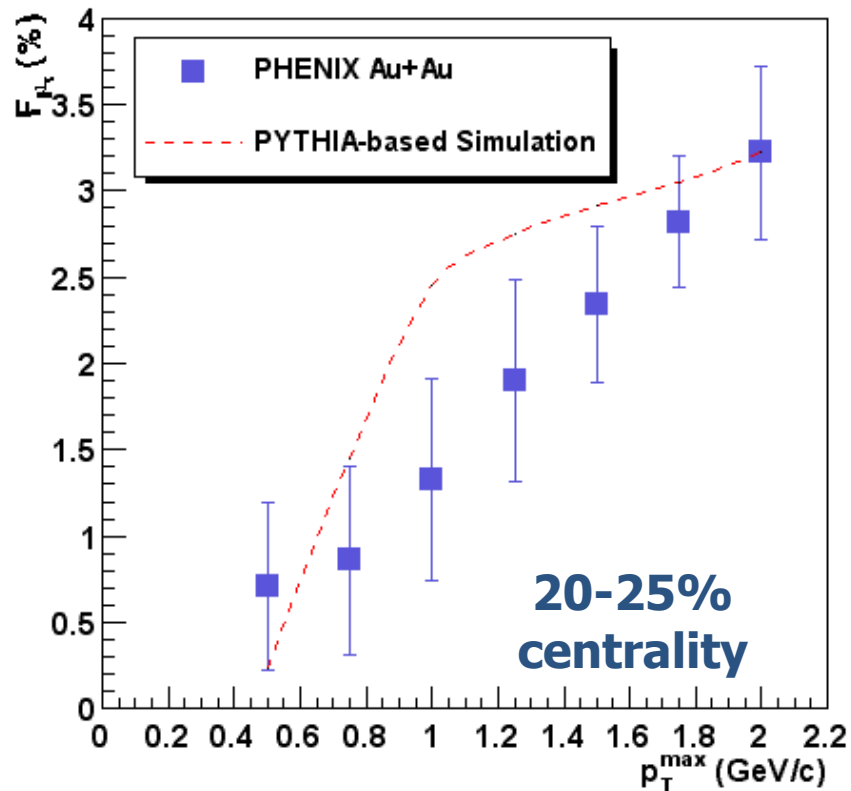
To mock up jet suppression,  $S_{\text{prob}}$  is scaled by the experimentally measured value of the nuclear modification factor,  $R_{\text{AA}}$ , as a function of centrality.

# Jet Simulation Results: PHENIX at $\sqrt{s_{NN}} = 200$ GeV

The  $S_{\text{prob}}$  parameter is initially adjusted so that  $F_{pT}$  from the simulation matches  $F_{pT}$  from the data for 20-25% centrality.



PHENIX Data: nucl-ex/0310005



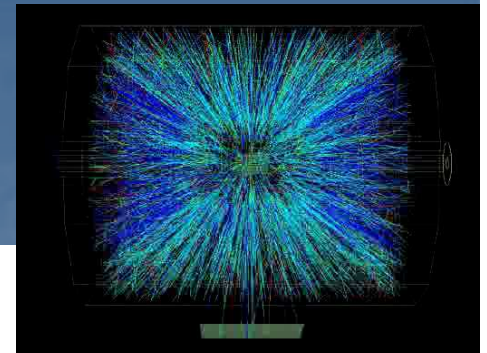
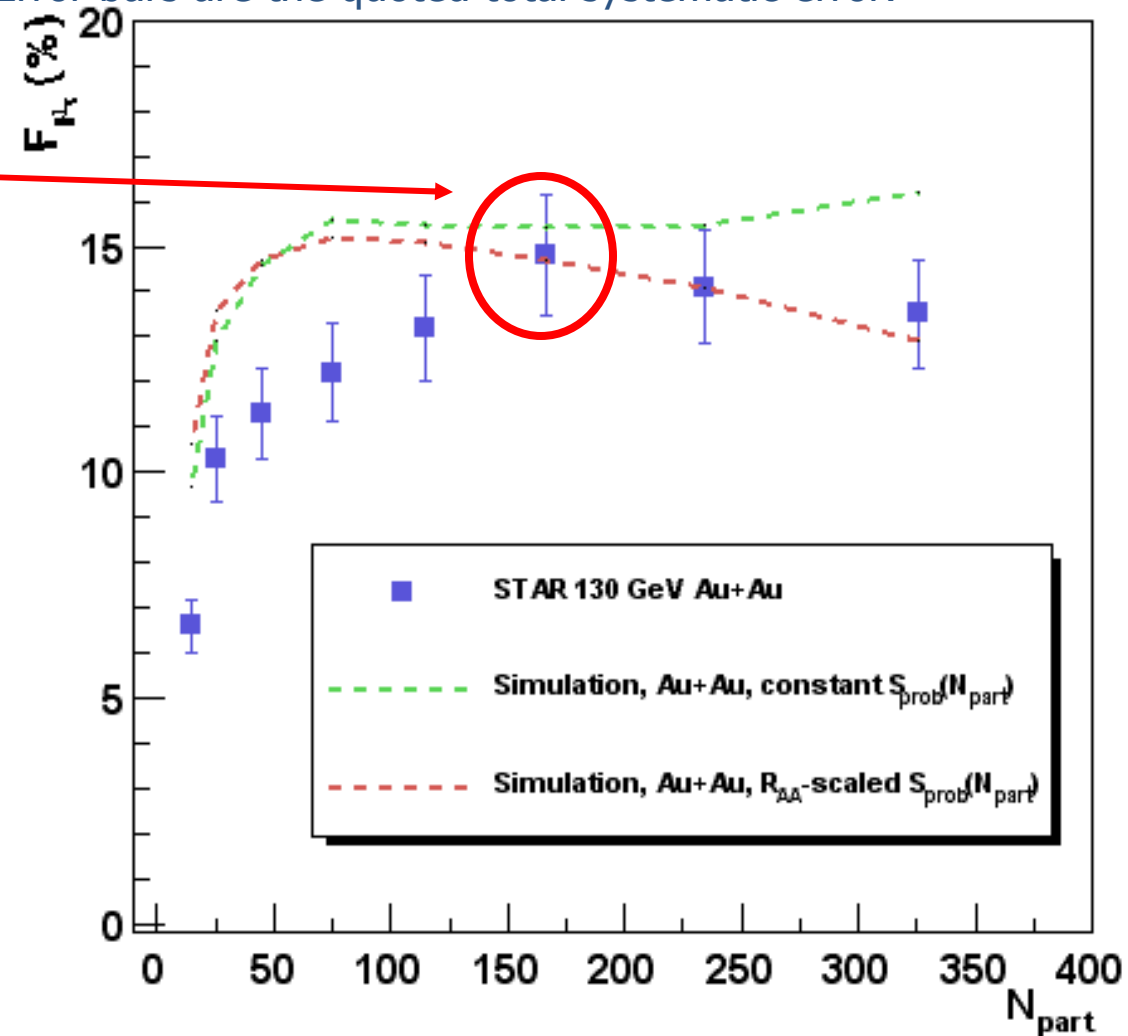
# Jet Simulation Results: STAR at $\sqrt{s_{NN}} = 130$ GeV

These results use the initial value of  $S_{\text{prob}}$  that matches the PHENIX data with the PYTHIA events filtered through the increased STAR acceptance. The measured STAR value of  $F_{pT}$  for 20-30% centrality is reproduced.

**PREDICTION: The STAR values of  $F_{pT}$  should increase by  $\sim 20\%$  for centralities 0-40% at  $\sqrt{s_{NN}} = 200$  GeV.**

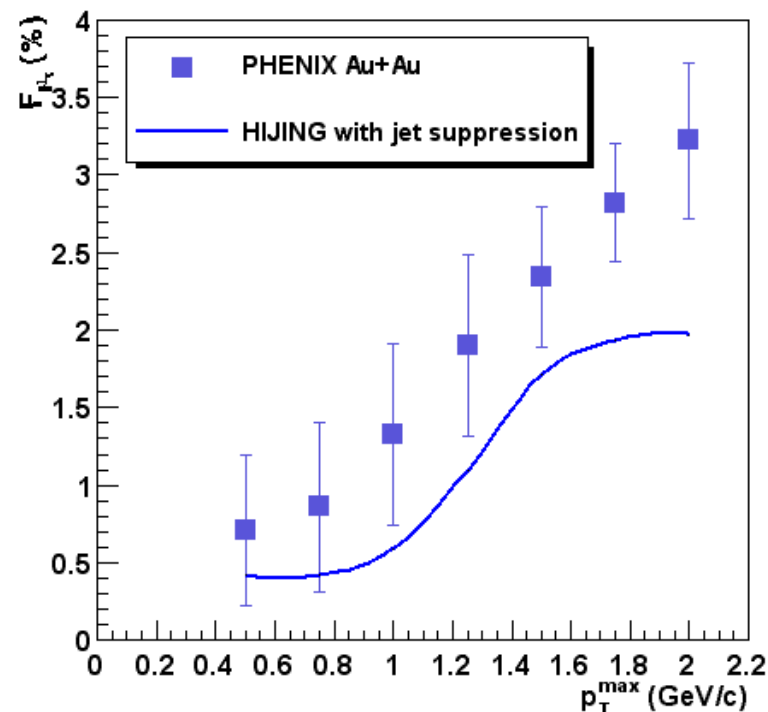
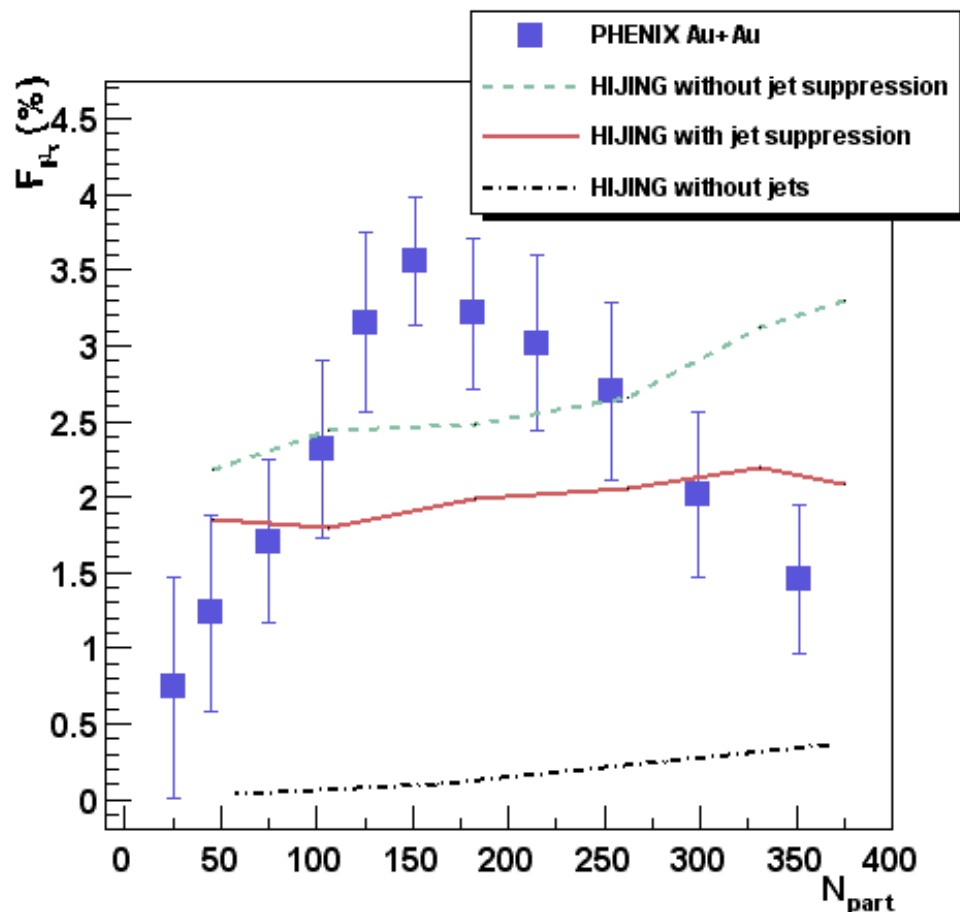
STAR data: nucl-ex/0308033

Error bars are the quoted total systematic error.





# Fluctuations According to HIJING



HIJING cannot reproduce the centrality dependence of the fluctuations.

One problem is that  $\langle N \rangle$  changes depending on the HIJING settings – not matched to the observed dataset.

Example for 0-5% centrality:  $\langle N \rangle = 93.0$  for jet suppression, 76.6 without suppression, and 51.2 without jets.

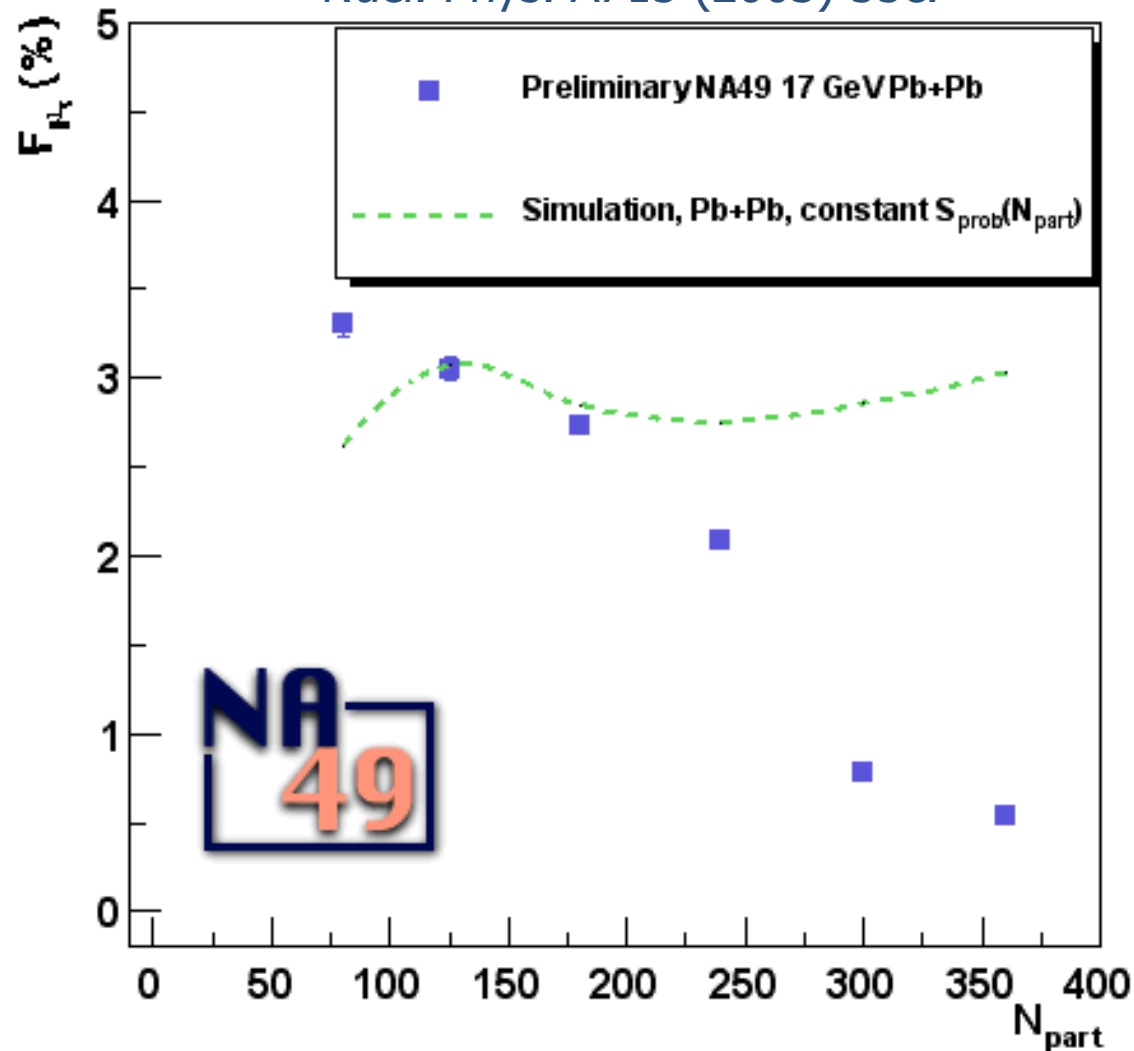
# Jet Simulation Results: NA49 at $\sqrt{s_{NN}} = 17$ GeV

Minimum bias p+p  
Data (NA49  
Published, Phys.  
Lett. B459 (1999)  
679):  
 $F_{pT} = 1.3\% \pm 0.26\%$

From PYTHIA min.  
bias p+p alone:  
 $F_{pT} = 2.3\%$

$S_{\text{prob}}$  must be scaled  
down by a factor of  
3.63 to match the  
most central data  
point.

NA49 Preliminary Data: C. Blume, et al.,  
Nucl. Phys. A715 (2003) 55c.



# Jet Simulation Results: CERES at $\sqrt{s_{NN}} = 17$ GeV

Energy dependence study:

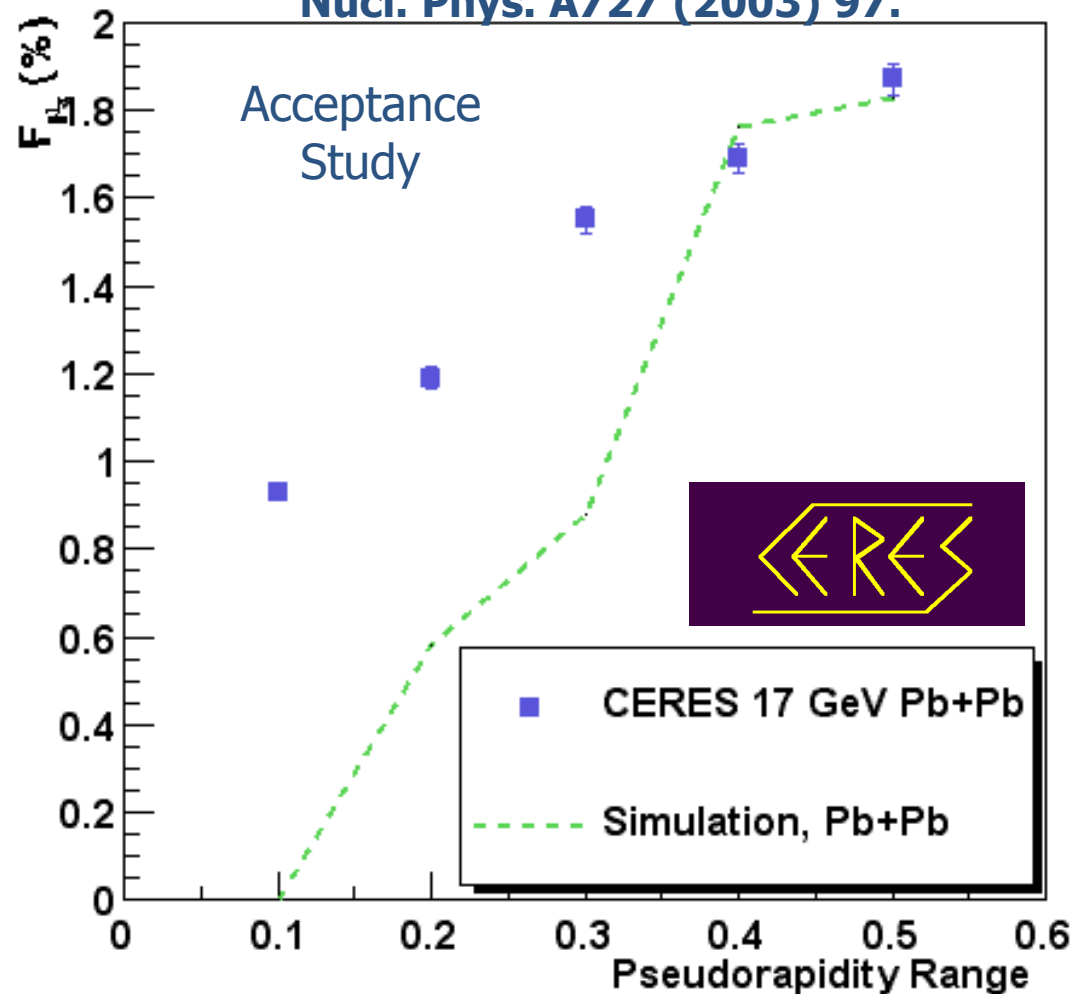
CERES data:  
 $F_{pT}(80 \text{ A GeV/c})/F_{pT}(158 \text{ A GeV/c}) = 0.72$

Simulation:  
 $F_{pT}(80 \text{ A GeV/c})/F_{pT}(158 \text{ A GeV/c}) = 0.72$

*Averaged over 0-30% centrality.*

CERES Data: D. Adamova, et al.,

Nucl. Phys. A727 (2003) 97.



# Estimate of the Magnitude of Event-by-Event Temperature Fluctuations

$$\frac{\sigma_T}{\langle T \rangle} = \sqrt{\frac{2F_{p_T}}{p(\langle N \rangle - 1)}}$$

R. Korus and S. Mrowczynski,  
Phys. Rev. C64 (2001) 054908.

Measurement	sqrt(s <sub>NN</sub> )	$\sigma_T/\langle T \rangle$ Most central	$\sigma_T/\langle T \rangle$ , At the peak
PHENIX	200	1.8%	3.7%
STAR	130	1.7%	3.8%
CERES	17	1.3%	2.2%
NA49	17	0.6%	2.6%

# Conclusions



- A simulation for studying the sources of event-by-event average  $p_T$  fluctuations has been described.
- A hybrid simulation using PYTHIA events to simulate hard process products can well reproduce the trends in fluctuation data at RHIC energies.
- The hybrid simulation predicts  $\sim 20\%$  increase in non-random fluctuations measured by STAR at 200 GeV compared to the 130 GeV results.
- The hybrid simulation can describe the energy dependence of the CERN data, but fails to describe the centrality- or pseudorapidity-acceptance-dependence.
- Estimates of the remaining signal available for temperature fluctuations are less than 2% for both RHIC and CERN energies.